

## Design and Selection of Programming Languages

### Operational Semantics Rules

$$\begin{array}{l}
 \text{Assignment: } \frac{\sigma(e) \Rightarrow v}{\sigma(x := e) \Rightarrow \sigma \oplus \{x \mapsto v\}} \qquad \text{Sequence: } \frac{\sigma_1(s_1) \Rightarrow \sigma_2 \quad \sigma_2(s_2) \Rightarrow \sigma_3}{\sigma_1(s_1; s_2) \Rightarrow \sigma_3} \\
 \\
 \text{Conditional: } \frac{\sigma(b) \Rightarrow \text{True} \quad \sigma(s_1) \Rightarrow \sigma_1}{\sigma(\text{if } b \text{ then } s_1 \text{ else } s_2 \text{ fi}) \Rightarrow \sigma_1} \quad \frac{\sigma(b) \Rightarrow \text{False} \quad \sigma(s_2) \Rightarrow \sigma_2}{\sigma(\text{if } b \text{ then } s_1 \text{ else } s_2 \text{ fi}) \Rightarrow \sigma_2} \\
 \\
 \text{while: } \frac{\sigma(b) \Rightarrow \text{True} \quad \sigma(s) \Rightarrow \sigma_1 \quad \sigma_1(\text{while } b \text{ do } s \text{ od}) \Rightarrow \sigma_2}{\sigma(\text{while } b \text{ do } s \text{ od}) \Rightarrow \sigma_2} \quad \frac{\sigma(b) \Rightarrow \text{False}}{\sigma(\text{while } b \text{ do } s \text{ od}) \Rightarrow \sigma}
 \end{array}$$

### Axiomatic Semantics Rules

$$\text{Assignment: } \{ P[x_1 \setminus e_1, \dots, x_n \setminus e_n] \} (x_1, \dots, x_n) := (e_1, \dots, e_n) \{ P \}$$

$$\text{Logical consequence: } \frac{P \Rightarrow P' \quad \{ P' \} S \{ Q' \} \quad Q' \Rightarrow Q}{\{ P \} S \{ Q \}}$$

$$\text{Sequence: } \frac{\{ P \} S_1 \{ R \} \quad \{ R \} S_2 \{ Q \}}{\{ P \} S_1 ; S_2 \{ Q \}}$$

$$\text{Conditional: } \frac{\{ P \wedge b \} S_1 \{ Q \} \quad \{ P \wedge \neg b \} S_2 \{ Q \}}{\{ P \} \text{ if } b \text{ then } S_1 \text{ else } S_2 \text{ fi } \{ Q \}}$$

$$\text{while-Loop: } \frac{\{ INV \wedge b \} S \{ INV \}}{\{ INV \} \text{ while } b \text{ do } S \text{ od } \{ INV \wedge \neg b \}}$$

$$\text{Assignment Tactics: } \frac{\frac{\langle\langle \text{Reasoning} \rangle\rangle}{P \Rightarrow Q[x \setminus e]} \quad \frac{\text{True}}{\{ Q[x \setminus e] \} x := e \{ Q \}} \text{ (Assignment Ax .)}}{\{ P \} x := e \{ Q \}} \text{ (Left Cons .)}$$

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module SimPLEval where
import SimPL
import qualified Data.Map as Map
import Data.Map (Map) -- only the type constructor is imported unqualified

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data Value1 = Vallnt Integer | ValBool Bool
type State1 = Map Variable Value1

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evalExpr :: Expression → State1 → Maybe Value1
evalExpr (Var v) s = Map.lookup v s
evalExpr (Value (LitInt i)) s = Just (Vallnt i) -- better: function litToVal
evalExpr (Value (LitBool b)) s = Just (ValBool b)
evalExpr (Binary (MkArithOp op) e1 e2) s = case (evalExpr e1 s, evalExpr e2 s) of
  (Just (Vallnt v1), Just (Vallnt v2)) → evalArithOp op v1 v2
  _ → Nothing
evalExpr (Binary (MkRelOp op) e1 e2) s = case (evalExpr e1 s, evalExpr e2 s) of
  (Just (Vallnt v1), Just (Vallnt v2)) → evalRelOp op v1 v2
  _ → Nothing
evalExpr (Binary (MkBoolOp op) e1 e2) s = case (evalExpr e1 s, evalExpr e2 s) of
  (Just (ValBool b1), Just (ValBool b2)) → evalBoolOp op b1 b2
  _ → Nothing
evalExpr (Unary Not e) s = case evalExpr e s of
  Just (ValBool b) → Just (ValBool (not b))
  _ → Nothing

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evalArithOp :: ArithOp → Integer → Integer → Maybe Value1
evalRelOp :: RelOp → Integer → Integer → Maybe Value1
evalBoolOp :: BoolOp → Bool → Bool → Maybe Value1
-- implementations omitted since not relevant for Final

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interpStmt :: Statement → (State1 → Maybe State1)
interpStmt (Assignment var e) s = case evalExpr e s of
  Just val → Just (Map.insert var val s)
  Nothing → Nothing
interpStmt (Conditional cond sThen sElse) s = case evalExpr cond s of
  Just (ValBool True) → (interpStmt sThen) s
  Just (ValBool False) → (interpStmt sElse) s
  _ → Nothing
interpStmt (Loop cond body) s = case evalExpr cond s of
  Just (ValBool False) → Just s
  Just (ValBool True) → case interpStmt body s of
    Just s1 → interpStmt (Loop cond body) s1
    _ → Nothing
  Just (Vallnt i) → Nothing
  Nothing → Nothing
interpStmt (MkBlock stmts) s = interpBlock stmts s

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interpBlock :: [Statement] → (State1 → Maybe State1)
interpBlock [] = Just
interpBlock (stmt : stmts) = λ s → case interpStmt stmt s of
  Just s1 → interpBlock stmts s1
  Nothing → Nothing

```